# Rovibrational Spectral Analysis of  $CO<sub>3</sub>$  and  $C<sub>2</sub>O<sub>3</sub>$ : Potential Sources for  $O<sub>2</sub>$  Observed in Comet 67P/Churyumov–Gerasimenko

Ryan C. Fortenberry<sup>[1](https://orcid.org/0000-0003-4716-8225)</sup> (D), Daniel Peters<sup>1</sup>, Brian C. Ferrari<sup>2</sup>, and Christopher J. Bennett<sup>2</sup>

<sup>1</sup> Department of C[hem](https://orcid.org/0000-0003-4716-8225)istry & Biochemistry, University of Mississippi, University, MS 38677-1848, USA; [r410@olemiss.edu](mailto:r410@olemiss.edu) <sup>2</sup> Department of Physics, University of Central Florida, Orlando, FL 32816, USA

Received 2019 August 5; revised 2019 October 26; accepted 2019 November 4; published 2019 November 15

# Abstract

The recent ROSETTA mission to comet 67P/Churyumov–Gerasimenko detected surprisingly high levels of molecular oxygen (O<sub>2</sub>; hypervolatile species) in the coma. Current models predict that considerable levels of other hypervolatiles (such as molecular nitrogen,  $N_2$ , methane,  $CH_4$ , and Argon) should be found at similar levels, whereas they are more depleted. One explanation explored here is that larger (less volatile) parent molecules may have been formed during radiolysis of cometary ices and, upon sublimation, are subsequently broken down within the coma into smaller, more volatile fragments. In support of this hypothesis, this work employs reliable quantum chemical techniques to provide the spectral data necessary for the detection of two candidate precursor "parent" molecules, cyclic carbon trioxide (c-CO<sub>3</sub>), and cyclic dicarbon trioxide (c-C<sub>2</sub>O<sub>3</sub>). Benchmark computations performed for gas-phase  $CO_2$  give vibrational frequencies to within 1.5 cm<sup>-1</sup> or better for the three fundamentals. Both c-CO<sub>3</sub> and c-C<sub>2</sub>O<sub>3</sub> have strong infrared features in the 4.5–5.5  $\mu$ m (1800–2200 cm<sup>-1</sup>) range and other notable infrared features closer to  $1100 \text{ cm}^{-1}$  (9.10  $\mu$ m). These molecules are both rotationally active, unlike CO<sub>2</sub>, and are therefore potentially observable and present new targets for radio telescope observations. Due to the stronger dipole moment, c-CO<sub>3</sub> should be more easily detectable than the nearly non-polar  $c$ -C<sub>2</sub>O<sub>3</sub>. These data may help observations of these molecules and can provide insights as to how radiation-driven derivatization of  $CO/CO<sub>2</sub>$ precursors could contribute to the generation of higher-mass parent species that subsequently degrade to produce more volatile species, such as  $O_2$ , observed in cometary comae.

Unified Astronomy Thesaurus concepts: [Astrochemistry](http://astrothesaurus.org/uat/75) (75); [Molecular spectroscopy](http://astrothesaurus.org/uat/2095) (2095); [Comets](http://astrothesaurus.org/uat/280) (280)

### 1. Introduction

In 2015 abundant molecular oxygen was discovered in comet 67P/Churyumov–Gerasimenko (hereafter, 67P) during the Rosetta mission (Bieler et al. [2015](#page-5-0)). Speculation as to the origins of this material vary since most of the  $O_2$  known to exist in the Earths atmosphere is believed to be of biological provenance, which cannot be the case in the interplanetary medium. Prior to encounter, chemical models (Glinski et al. [2004;](#page-6-0) Pierce & A'Hearn [2010](#page-6-0)) predicted that some  $O_2$  could be formed in the comae of comets, but not to the levels detected by Rosetta. The observations, and several suggested mechanisms for  $O_2$  production in comet 67P, have been reviewed recently (Luspay-Kuti et al. [2018;](#page-6-0) Altwegg et al. [2019](#page-5-0)). Several authors have suggested that the  $O_2$  detected could be primordial to the solar system and is being released as molecular  $O_2$  as the comet approaches perihelion. However, many of these models require adoption of specific parameters to favor  $O_2$  production (e.g., higher densities, higher temperatures, higher galactic cosmic radiation rates), while hindering the production of other species, such as ozone,  $O_3$ , hydrogen dioxide,  $HO_2$ , and hydrogen peroxide,  $H_2O_2$  (Taquet et al. [2016;](#page-6-0) Heritier et al. [2018;](#page-6-0) Laufer et al. [2018;](#page-6-0) Eistrup & Walsh [2019](#page-5-0)). However, under these considerations, the simultaneous preservation of primordial  $O_2$  alongside the depletion of other hypervolatile species, such as molecular nitrogen,  $N_2$ , methane, CH<sub>4</sub>, and argon remains challenging to explain since mechanisms such as selective trapping or clathrate formation are unlikely.

Other explanations are more focused on ways to form  $O_2$  at a later stage, or in situ within the coma. The formation of  $O_2$ from the dismutation of  $H_2O_2$  has also been suggested (Dulieu et al.  $2017$ ), but the required levels of  $H_2O_2$  needed to explain

the formation of  $O_2$  by this mechanism are several orders higher than those observed in 67P. Others have suggested that  $O<sub>2</sub>$  forms from interactions of water pick-up ions with the oxidized surface of the rock substrate or grains subsumed in the icy mantle (Yao & Giapis [2017](#page-6-0)) where energetic  $O_2^-$  anions would be the primary product released. Consequently, doubt that such species could be produced in enough abundance to generate the amounts of  $O_2$  in question, as well as whether energetic  $O_2^-$  anions would have been detectable, have been raised (Heritier et al. [2018](#page-6-0)). Furthermore, another intermediate in this surface-catalyzed reaction is the so-called "oxywater" molecule  $(H<sub>2</sub>O-O)$ , but the stability of this neutral species has been questioned for some time (Meredith et al. [1992](#page-6-0); Xie et al. [1996;](#page-6-0) Franz et al. [2009](#page-5-0)). Differently, the oxywater cation  $(H<sub>2</sub>OO<sup>+</sup>)$  has been proposed as the progenitor of the O–O bond through reaction of water cations with atomic oxygen leading to an electronically excited state favoring creation of  $O_2^+$  and H<sub>2</sub> (Fortenberry et al. [2019](#page-5-0)). This reaction has only been proposed theoretically, and likely low abundances of  $H<sub>2</sub>O<sup>+</sup>$  in 67P may hinder such a process (Fuselier et al. [2016](#page-6-0)). The potential build-up of  $O_2$  from irradiated water ices has been suggested (Mousis et al. [2018](#page-6-0)), but the radiolytic yields of  $O<sub>2</sub>$  production within pure water are too low to explain the observations (Zheng et al. [2006](#page-6-0)). Due to these considerations, it may be more likely that the irradiation of other ices besides H2O could play important roles. For example, the production of  $O_2$  within carbon dioxide  $(CO_2)$  ices is often considerably higher (Martín-Doménech et al. [2015](#page-6-0)), and this ice can be present at levels up to 20% in comets. However, the observations at 67P were consistent with the interpretation that the  $O_2$  signal appears to be correlated with the release of H2O (Altwegg et al. [2019](#page-5-0)).



An alternative view of what is occurring is that what is being observed as  $O_2$  by the mass spectrometer may not likely start out as  $O_2$ . Instead, it is conceivable that larger, less volatile "parent" species that are produced during the radiolysis of ices are sublimating alongside the  $H_2O$  molecules—since they have similar volatility to water—and are then being subsequently degraded. The breakdown of these molecules may occur because these species are unstable in the gas-phase, or due to processes occurring within the cometary coma or within the mass spectrometer. The breakdown of large molecular species has been suggested to account for distributed sources, observed for several molecules (Cottin & Fray [2008](#page-5-0)). In fact, carbon oxide species, such as carbon suboxide  $(C_2O_3)$ , have been suggested to account for distributed sources of CO and dicarbon monoxide  $(C_2O)$  (Huntress et al. [1991](#page-6-0); Bennett et al. [2008](#page-5-0)), for example.

Here, the potential contribution of larger carbon oxide species produced during the radiolysis of  $CO<sub>2</sub>$  ices are investigated to see if they may then sublimate later (i.e., alongside water) and then could potentially contribute to the observed  $O_2$  signal at comet 67P as they are broken down. The simplest such molecule beyond  $CO<sub>2</sub>$  itself is carbon trioxide, CO<sub>3</sub>. The most stable form is the cyclic  $C_{2v}$  molecule, which also happens to be the most abundant form observed produced during the radiolysis of  $CO<sub>2</sub>$  ices by ultraviolet (UV) photons (Moll et al. [1966;](#page-6-0) Gerakines et al. [1996;](#page-6-0) Martín-Doménech et al. [2015](#page-6-0); Radhakrishnan et al. [2018](#page-6-0)), energetic electrons (e.g., Bennett et al. [2004](#page-5-0)), and energetic ions (Bennett et al. [2014,](#page-5-0) and references therein). The less abundant  $D_{3h}$  isomer of carbon trioxide has been identified (Jamieson et al. [2006](#page-6-0)), along with the  $C_{2v}$  form of carbon tetraoxide (CO<sub>4</sub>; Jamieson et al.  $2007b$ ), the  $C_2$  form of carbon pentaoxide (CO<sub>5</sub>; Jamieson et al. [2007a](#page-6-0)), and the  $C_s$  form of carbon hexaoxide (CO<sub>6</sub>; Jamieson et al.  $2008$ ) alongside CO, O<sub>2</sub>, and ozone (O<sub>3</sub>). Note that although  $CO<sub>3</sub>$  is one of the most abundant species formed within these ices, the  $CO<sub>3</sub><sup>+</sup>$  (with a mass-to-charge ratio,  $m/z = 60$ ) ion is not typically identified by mass spectrometry during sublimation of irradiated  $CO<sub>2</sub>$  ices in these laboratory investigations. This indicates that  $CO<sub>3</sub>$  likely dissociates either directly upon sublimation or perhaps it fragments easily when subjected to UV photons or energetic electrons present in the cometary comae; in either case, abundant  $O_2$  and CO (or  $CO_2$ ) and O) could be produced. Additionally, a  $m/z = 60$  peak in the Rosetta data is currently attributed to OCS with a mass of 59.966985 amu.  $CO<sub>3</sub>$  has a mass of 59.984745 amu (Altwegg & Team [2018](#page-5-0)), making their difference right at the limit of what is discernable giving some evidence that  $CO<sub>3</sub>$  may be present in 67P or similar comets.

Another relatively simple molecule that could sublime from an irradiated  $CO<sub>2</sub>$  surface is oxalic anhydride,  $C<sub>2</sub>O<sub>3</sub>$ . This molecule has been suggested to be formed when CO is exposed to high pressures, alongside carbon suboxide  $(C_3O_2; Lipp$  et al. [1998](#page-6-0)), which has been suggested as a parent molecular species that could potentially contribute to the extended source of CO as well as dicarbon  $(C_2)$  and dicarbon monoxide  $(C_2O;$ Huntress et al.  $1991$ ; Bennett et al.  $2008$ ). The  $C_2O_3$  molecule is investigated here since it has not been well characterized previously but could potentially be produced during  $CO<sub>2</sub>$ irradiation experiments, as evidenced by its infrared absorption bands derived here. This molecule is roughly triangular of  $C_{2v}$ symmetry as shown in Figure [1](#page-2-0) and is of the same connectivity

as the closely related NCNCN<sup>−</sup> molecule recently studied (Dubois et al. [2019](#page-5-0)). Relatively little is known about this molecule, but the proximity of the two outlying oxygen atoms makes them prime targets for gas-phase collisional reactions with other, exposed oxygen species. Such reactions, again, would lead to additional  $O_2$  (and more  $CO/CO_2$ ).

In any case,  $CO_3$  and  $C_2O_3$  likely dissociate either at or shortly after sublimation and will have short lifetimes in situ making their abundances consistent with the amount of volatiles observed correlating to  $O_2$  (Altwegg & Team [2018](#page-5-0)). Consequently, if these molecules are to be considered as possible intermediates in the formation of molecular oxygen from carbon dioxide ices, they must be detected in the gasphase in the laboratory and then in comae in situ. This work is relying upon trusted quantum chemical approaches to provide spectral data for these small,  $CO<sub>2</sub>$  derivatives. The expectation is that the data produced herein could serve as guides for the exploration that lower volatility radiation products produced primarily from  $CO<sub>2</sub>$  radiolysis could be contributing to the detected  $O_2$  yield.

#### 2. Computational Details

Coupled cluster theory at the singles, doubles, and perturbative triples level (Raghavachari et al. [1989](#page-6-0)) within the F12 explicitly correlated electron formalism (Adler et al. [2007;](#page-5-0) Knizia et al. [2009](#page-6-0)) and a triple-zeta basis set (Hill & Peterson [2010](#page-6-0)) is employed. Then, these CCSD(T)-F12b/ccpVTZ-F12 (hereafter, F12-TZ) energies are utilized within a fourth-order Taylor series expansion of the internuclear Hamiltonian's potential (or quartic force field (QFF)) to produce the spectroscopic data. Such an approach has been shown previously to match higher-level computations exceptionally well (Agbaglo et al. [2019](#page-5-0); Agbaglo & Fortenberry [2019a](#page-5-0), [2019b](#page-5-0)) including NCNCN<sup>−</sup> (Dubois et al. [2019](#page-5-0)). Similar computational analysis has also preceded subsequent experimental and astronomical detection of various molecules (Huang et al. [2011](#page-6-0); Fortenberry et al. [2012](#page-5-0); Zhao et al. [2014](#page-6-0); Theis & Fortenberry [2016](#page-6-0); Bizzocchi et al. [2017](#page-5-0); Fortenberry & Francisco [2017](#page-5-0); Fuente et al. [2017;](#page-5-0) Wagner et al. [2018](#page-6-0)).

The QFFs begin with geometry optimizations of each molecule with the F12-TZ approach. Then, energy points are created with displacements of  $\pm 0.005 \text{ Å}$  for bond lengths and  $\pm 0.005$  radians from this reference geometry in order to compute the numerical derivatives up to fourth-order. At each point, the F12-TZ energies are computed. All F12-TZ computations use the MOLPRO 2015.1 quantum chemical program (Werner et al. [2012,](#page-6-0) [2015](#page-6-0)). A least-squares fit produces the equilibrium geometry, and a refit produces the necessary force constants. The INTDER program (Allen et al. [2005](#page-5-0)) transforms the symmetry-internal coordinates for each molecule (defined below) into Cartesian coordinates for generic use within the SPECTRO program (Gaw et al. [1991](#page-6-0)). Secondorder rotational (Mills [1972](#page-6-0)) and vibrational perturbation theory (VPT2; Watson [1977](#page-6-0); Papousek & Aliev [1982](#page-6-0)) are utilized therein to produce the spectroscopic constants and vibrational frequencies.

CO<sub>2</sub> is exhibiting the known  $2\nu_3 = \nu_2$  type-1 Fermi resonance which is accounted for in the VPT2 computations within SPECTRO. CO<sub>3</sub> has a  $2\nu_3 = 2\nu_2 = \nu_1$  Fermi resonance polyad, as well as a  $2\nu_5 = \nu_2$  type-1 Fermi resonance and a  $\nu_6 + \nu_5 = \nu_3$  type-2 Fermi resonance.  $\nu_6/\nu_5$  C-type and

<span id="page-2-0"></span>

**Figure 1.** CCSD(T)-F12/cc-pVTZ-F12 equilibrium geometry (in  $\AA$  and  $\degree$ ) of  ${}^{1}A_1$  C<sub>2</sub>O<sub>3</sub>.

 $\nu_6/\nu_4$  A-type Coriolis resonances are also present. C<sub>2</sub>O<sub>3</sub> possesses  $2v_3 = v_4 + v_3 = v_7 + v_2 = v_1$ ,  $2v_5 = v_7 + v_6 =$  $\nu_9 + \nu_4 = \nu_3$ ; and  $2\nu_7 = 2\nu_8 = \nu_4$  Fermi resonance polyads. It further has  $\nu_6 + \nu_3 = \nu_2$ ,  $\nu_8 + \nu_7 = \nu_5$ , and  $\nu_9 + \nu_7 = \nu_6$ type-2 Fermi resonances as well as  $\nu_6/\nu_5$  A-type,  $\nu_9/\nu_7$  C-type, and  $\nu_9/\nu_8$  A-type Coriolis resonances. The intensities are computed with MP2/6-31 +  $G^*$  in the Gaussian09 program (Møller & Plesset [1934;](#page-6-0) Hehre et al. [1972;](#page-6-0) Frisch et al. [2009](#page-5-0)) shown previously to give good results compared to higherorder computations (Yu et al. [2015](#page-6-0); Finney et al. [2016](#page-5-0)).

The symmetry-internal coordinates for  $CO<sub>2</sub>$  are simply: (1) the  $C=O$  symmetric stretch, (2) the  $C=O$  antisymmetric stretch, and  $3/4$ ) the bend(s). The symmetry-internal coordinates for  $CO<sub>3</sub>$  are below with atoms numbered relative to Figure 2 with OPB is defined as the out-of-plane bend:

$$
S_1(a_1) = \mathbf{C} - \mathbf{O}_1 \tag{1}
$$

$$
S_2(a_1) = \frac{1}{\sqrt{2}}[(O_2 - C) + (O_3 - C)] \tag{2}
$$

$$
S_3(a_1) = \frac{1}{\sqrt{2}} [\angle (O_2 - C - O_1) + \angle (O_3 - C - O_1)] \quad (3)
$$

$$
S_4(b_2) = \frac{1}{\sqrt{2}}[(O_2 - C) - (O_3 - C)] \tag{4}
$$

$$
S_5(b_2) = \frac{1}{\sqrt{2}} [\angle (O_2 - C - O_1) - \angle (O_3 - C - O_1)] \quad (5)
$$

$$
S_6(b_1) = OPB(O_1 - C - O_2 - O_3). \tag{6}
$$

The symmetry-internal coordinates for  $C_2O_3$  with atoms numbered relative to Figure 1 are given as

$$
S_1(a_1) = C_1 - C_2 \tag{7}
$$

$$
S_2(a_1) = \frac{1}{\sqrt{2}} [(O_1 - C_1) + (O_1 - C_2)]
$$
 (8)

$$
S_3(a_1) = \frac{1}{\sqrt{2}}[(C_1 - O_2) + (C_2 - O_3)]
$$
 (9)

$$
S_4(a_1) = \frac{1}{\sqrt{2}} [\angle (O_2 - C_1 - O_1) + \angle (O_3 - C_2 - O_1)]
$$
\n(10)



**Figure 2.** CCSD(T)-F12/cc-pVTZ-F12 equilibrium geometry (in  $\hat{A}$  and  $\degree$ ) of  $A_1$  CO<sub>3</sub>.

$$
S_5(b_2) = \frac{1}{\sqrt{2}} [(O_1 - C_1) - (O_1 - C_2)] \tag{11}
$$

$$
S_6(b_2) = \frac{1}{\sqrt{2}}[(C_1 - O_2) - (C_2 - O_3)]
$$
 (12)

$$
S_7(b_2) = \frac{1}{\sqrt{2}} [\angle (O_2 - C_1 - O_1) - \angle (O_3 - C_2 - O_1)]
$$
\n(13)

$$
S_8(b_1) = \frac{1}{\sqrt{2}} [\tau (O_2 - C_1 - O_1 - C_2) - \tau (O_3 - C_2 - O_1 - C_1)]
$$
 (14)

$$
S_9(a_2) = \frac{1}{\sqrt{2}} [\tau (O_2 - C_1 - O_1 - C_2) + \tau (O_3 - C_2 - O_1 - C_1)]
$$
 (15)

where  $\tau$  represents the torsion/dihedral angle for the subsequent four atoms. This type of treatment has proven

#### Table 1

CCSD(T)-F12/cc-pVTZ-F12 Harmonic and Anharmonic (QFF) Rotational Constants (MHz), Dipole Moments (D), and Vibrational Frequencies (cm<sup>-1</sup>) with Intensities in Parentheses (km/mol) with Frequency Ordering from Highest to Lowest



Notes.<br><sup>a</sup> Data from Herzberg (1966), Shimanouchi (1972), Rothman et al. (1992).

<sup>b</sup> Data from Bennett et al. ([2004](#page-5-0)). <sup>c</sup> For CO<sub>2</sub>, these should be understood to be D and H as there is no branching in the linear molecule.

necessary in related systems (Fortenberry et al. [2017;](#page-5-0) Dubois et al. [2019](#page-5-0)).

### 3. Results and Discussion

As shown in Table 1 initial benchmarking with the carbon dioxide molecule is exceptional. The F12-TZ anharmonic vibrational frequencies are within 1.5 cm<sup>-1</sup> (0.03  $\mu$ m) or less for each of the three fundamental modes (Shimanouchi [1972](#page-6-0)) further corroborating the benchmarks for this level of theory with  $c$ -(C)C<sub>3</sub>H<sub>2</sub> and NCNCN<sup>-</sup> (Agbaglo et al. [2019](#page-5-0) and Dubois et al. [2019](#page-5-0)). The lower-level, double-harmonic computed intensities are also in semi-quantitative agreement and are certainly in the right proportion with one another. The experimentally inferred rotational constant of 11,698 MHz (Herzberg [1966](#page-6-0)) is within 40 MHz of the F12-TZ computations. Hence, the F12-TZ QFF results should be able to predict accurately the infrared and millimeter wave properties for observation of these possible  $CO<sub>2</sub>$  ice derivatives. It should also be noted that the vibrational modes are ordered by frequency

and not by symmetry in Table 1 for more direct comparison between molecules in the present study.

While there is much debate as to the ground state of  $CO<sub>3</sub>$ , this study will limit itself to the  $C_{2v}$  isomer. Part of this is due to convenience for the use of this symmetry and that the present computations put the  $D_{3h}$  isomer 0.27 eV higher in energy. Another reason for studying the  $C_{2v}$  isomer is the exceptionally bright  $\nu_1$  (a<sub>1</sub>) intensity for the C=O stretch at the apex of the molecule. This intensity is on the order of that for the antisymmetric stretch in carbon dioxide and will fall close to 2055.6 cm<sup>-1</sup> (4.86  $\mu$ m) in a spectral region of many lines but few even qualitative spectral assignments. This mode also exhibits no apparent anharmonicity, but such behavior results simply from proper inclusion of the  $2\nu_3 = 2\nu_2 = \nu_1$  Fermi resonance polyad (Martin & Taylor [1997](#page-6-0)). Additionally, previous experimental work on  $CO<sub>3</sub>$  indicates that the frequency at  $2045 \text{ cm}^{-1}$  (Bennett et al.  $2004$ ) is likely caused by the  $C_{2v}$  isomer due to the correlation of the experimental and theoretical values here. The antisymmetric  $\nu_3$  ( $b_2$ ) stretch at



<span id="page-4-0"></span>

CO <sub>2</sub>			CO <sub>3</sub>					$C_2O_3$		
$F_{44} = F_{33}$	0.786186	$F_{11}$	15.318271	$F_{552}$	$-0.6972$	$F_{5411}$	2.87	$F_{11}$	5.193773	
$F_{22}$	14.746201	$F_{21}$	1.117484	$F_{553}$	$-0.5130$	$F_{5421}$	1.29	$F_{21}$	$-0.011872$	
$F_{11}$	17.252686	$F_{22}$	8.147579	$F_{661}$	$-0.2110$	$F_{5422}$	$-0.59$	$F_{22}$	4.159832	
$F_{441} = F_{331}$	$-1.6586$	$F_{31}$	0.532870	$F_{662}$	$-5.2395$	$F_{5431}$	0.96	$F_{31}$	0.680483	
$F_{221}$	$-78.6236$	$F_{32}$	$-2.410035$	$F_{663}$	9.5412	$F_{5432}$	0.59	$F_{32}$	0.743305	
$F_{111}$	$-86.3217$	$F_{33}$	5.248298	$F_{1111}$	617.90	$F_{5433}$	$-2.96$	$F_{33}$	15.402199	
$F_{4444} = F_{3333}$	1.40	$F_{44}$	4.399800	$F_{2111}$	7.04	$F_{5444}$	3.75	$F_{41}$	0.006224	
$F_{4433}$	1.52	$F_{54}$	0.367289	$F_{2211}$	4.49	$F_{5511}$	0.89	$F_{42}$	$-0.004906$	
$F_{4422}$	$-1.94$	$F_{55}$	0.701563	$F_{2221}$	0.76	$F_{5521}$	1.87	$F_{43}$	0.032514	
$F_{3322}$	$-1.94$	$F_{66}$	0.779582	$F_{2222}$	139.50	$F_{5522}$	0.45	$F_{44}$	1.423942	
$F_{2222}$	309.19	$F_{111}$	$-107.8444$	$F_{3111}$	0.30	$F_{5531}$	1.39	$F_{55}$	1.493720	
$F_{4411} = F_{3311}$	2.85	$F_{211}$	$-3.1719$	$F_{3211}$	2.63	$F_{5532}$	0.48	$F_{65}$	1.260481	
$F_{2211}$	324.81	$F_{221}$	$-1.3879$	$F_{3221}$	1.99	$F_{5533}$	$-1.38$	$F_{66}$	14.804001	
$F_{1111}$	345.09	$F_{222}$	$-38.2000$	$F_{3222}$	$-20.12$	$F_{5544}$	$-1.10$	$F_{75}$	0.439303	
		$F_{311}$	$-1.2560$	$F_{3311}$	2.33	$F_{5554}$	0.59	$F_{76}$	0.207699	
		$F_{321}$	$-1.1362$	$F_{3321}$	1.08	$F_{5555}$	1.12	$F_{77}$	0.973483	
		$F_{322}$	10.0412	$F_{3322}$	38.09	$F_{6611}$	$-2.02$	$F_{88}$	0.215159	
		$F_{331}$	$-1.4607$	$F_{3331}$	0.47	$F_{6621}$	$-0.51$	$F_{99}$	0.271903	
		$F_{332}$	$-20.8658$	$F_{3332}$	$-116.79$	$F_{6622}$	18.91			
		$F_{333}$	56.4557	$F_{3333}$	362.60	$F_{6631}$	$-1.11$			
		$F_{441}$	$-1.1670$	$F_{4411}$	$-0.73$	$F_{6632}$	$-44.26$			
		$F_{442}$	$-26.9634$	$F_{4421}$	3.03	$F_{6633}$	130.98			
		$F_{443}$	$-4.6166$	$F_{4422}$	118.41	$F_{6644}$	$-6.55$			
		$F_{541}$	$-1.1976$	$F_{4431}$	6.26	$F_{6654}$	0.19			
		$F_{542}$	$-0.2886$	$F_{4432}$	15.83	$F_{6655}$	2.59			
		$F_{543}$	$-0.6107$	$F_{4433}$	$-41.28$	$F_{6666}$	52.16			
		$F_{551}$	$-1.1297$	$F_{4444}$	119.69					

Table 3 CCSD(T)-F12/cc-pVTZ-F12 Cubic and Quartic Force Constants for  $C_2O_3$  in mdyne/ $(\AA^n rad^m)$ 



<span id="page-5-0"></span>

(Continued)										
$F_{751}$	1.7670	$F_{4321}$	0.240	$F_{6641}$	$-1.868$	$F_{7765}$	1.548	$F_{9943}$	$-0.092$	
$F_{752}$	$-0.6787$	$F_{4322}$	0.917	$F_{6642}$	1.879	$F_{7766}$	0.700	$F_{9944}$	$-0.280$	
$F_{753}$	$-0.7817$	$F_{4331}$	$-0.982$	$F_{6643}$	$-0.169$	$F_{7775}$	0.435	$F_{9955}$	0.300	
$F_{754}$	$-1.3130$	$F_{4332}$	0.883	$F_{6644}$	0.391	$F_{7776}$	0.829	$F_{9965}$	0.028	
$F_{761}$	1.2312	$F_{4333}$	$-0.425$	$F_{6655}$	$-0.421$	$F_{7777}$	1.662	$F_{9966}$	0.125	
$F_{762}$	$-1.1078$	$F_{4411}$	$-1.457$	$F_{6665}$	2.637	$F_{8811}$	0.255	$F_{9975}$	$-0.066$	
$F_{763}$	$-0.3939$	$F_{4421}$	1.071	$F_{6666}$	309.821	$F_{8821}$	$-0.231$	$F_{9976}$	0.233	
$F_{764}$	$-1.1753$	$F_{4422}$	$-0.452$	$F_{7511}$	$-2.123$	$F_{8822}$	0.025	$F_{9977}$	$-0.230$	
$F_{771}$	$-1.2774$	$F_{4431}$	0.457	$F_{7521}$	$-0.475$	$F_{8831}$	0.385	$F_{9988}$	0.082	
$F_{772}$	$-0.5040$	$F_{4432}$	2.082	$F_{7522}$	1.240	$F_{8832}$	0.027	$F_{9999}$	0.256	
$F_{773}$	$-0.9564$	$F_{4433}$	0.389							

Table 3

965.0 cm<sup>-1</sup> (10.36  $\mu$ m) is roughly 25% of the intensity of  $\nu_1$ implying that it will also create a notable transition in any spectrum and is within  $8 \text{ cm}^{-1}$  of the attributed peak from the same referenced experiment (Bennett et al. 2004). The other vibrational modes are relatively dim and are shifted toward the far-infrared, but correlation between the present theoretical and previous experimental  $\nu_2$  and  $\nu_6$  fundamentals are noteworthy differing between the two approaches by less than  $3 \text{ cm}^{-1}$  in each case. Hence, the previous experimental work on  $CO<sub>3</sub>$  is likely for the  $C_{2v}$  isomer. Regardless, the 0.70 D dipole moment of  $CO<sub>3</sub>$  may also make it detectable with radio telescopes from the ground unlike its linear  $CO<sub>2</sub>$  cousin.

The force constants, given in Tables [2](#page-4-0) and [3,](#page-4-0) show that the  $C=O<sub>1</sub>$  bond, ordered from Figure [2,](#page-2-0) at the apex of the molecule  $(F_{11}$  at 15.318 mdyne/ $\AA^2$ ) is bonded much more strongly than the two externally, exposed oxygen atoms  $(O_2 \text{ and } O_3)$  at each side ( $F_{22}$  8.148 mydne/ $\AA^2$ ). Hence, the bond order for the apical C=O bond is nearly twice that for the other two C−O indicative of double bonds in the ketone moiety at the apex, and single bonds on the sides. The  $F_{33}$  force constant of 5.248 mydne/Å<sup>2</sup> also implies a single O<sub>2</sub>−O<sub>3</sub> bond at the bottom of the molecule in Figure [2.](#page-2-0) In any case, vibrational excitation of the  $\nu_5$  (a<sub>1</sub>) symmetric bend at 686.1 cm<sup>-1</sup> (14.58  $\mu$ m) could further promote bonding between the two symmetric oxygen atoms leading to formation of molecular oxygen and CO.

The  $C_2O_3$  molecule has even more bright infrared fundamental vibrational frequencies. All of the stretches above  $1100 \text{ cm}^{-1}$  (9.10  $\mu$ m) have large intensities. Most notably, the 1857.8 cm<sup>-1</sup> (5.38  $\mu$ m)  $\nu$ <sub>2</sub> ( $\overline{b}$ <sub>2</sub>) antisymmetric C=O stretch involving the external  $O_2$  and  $O_3$  atoms is, again, on the order of the antisymmetric stretch in carbon dioxide. The two other stretches in this frequency region are once more roughly 25% of this bright mode. However, the  $\nu_8$  ( $b_1$ ) out-of-plane bend at 339.5 cm<sup> $-1$ </sup> (29.46  $\mu$ m) also has an intensity of this magnitude. The 0.09 D dipole moment implies that this molecule is also detectable via radio telescopes in theory, but the low value is not as promising for detection as the infrared bands should be.

#### 4. Conclusions

In order to detect either of these molecules as possible precursors to  $O_2$  formation in comet 67P, the spectral data provided here are essential. Furthermore, the previous experimental work on  $CO<sub>3</sub>$  gives indication of originating with the  $C_{2v}$  isomer.  $CO_3$  and  $C_2O_3$  have bright infrared bands in littleunderstood regions of the mid-infrared and have detectable dipole moments and corroborate the available experimental data. Additionally, the exposed oxygen atoms in both molecules could be donated to other oxygen atoms creating  $O_2$ .  $CO_3$  should do this more readily since  $O_2$  could form directly from this molecule due to the existence of a seeming O −O bond and relatively weak C−O bonds. The external C=O bonds in  $C_2O_3$  are fairly strong, and do not have a corresponding vibrational fundamental leading to O−O bond formation. In any case, the data provided here will allow these novel molecules to be detected either in the laboratory or in cometary environments and could shed light onto the formation of  $O_2$  in comet 67P.

R.C.F. acknowledges funding from NASA grant NNX17AH15G, NSF grant OIA-1757220, and start-up funds provided by the University of Mississippi. C.J.B. acknowledges funding from the NASA Solar System Exploration Research Virtual Institute CLASS (NNA14AB05A).

#### ORCID iDs

# R[y](https://orcid.org/0000-0003-4716-8225)an C. Fortenberry **[https:](https://orcid.org/0000-0003-4716-8225)//orcid.org/[0000-0003-](https://orcid.org/0000-0003-4716-8225)** [4716-8225](https://orcid.org/0000-0003-4716-8225)

#### References

- Adler, T. B., Knizia, G., & Werner, H.-J. 2007, [JChPh](https://doi.org/10.1063/1.2817618), [127, 221106](https://ui.adsabs.harvard.edu/abs/2007JChPh.127v1106A/abstract)
- Agbaglo, D., & Fortenberry, R. C. 2019a, [IJQC,](https://doi.org/10.1002/qua.25899) 119, e25899
- Agbaglo, D., & Fortenberry, R. C. 2019b, [CPL,](https://doi.org/10.1016/j.cplett.2019.136720) [734, 136720](https://ui.adsabs.harvard.edu/abs/2019CPL...73436720A/abstract)
- Agbaglo, D., Lee, T. J., Thackston, R., & Fortenberry, R. C. 2019, [ApJ](https://doi.org/10.3847/1538-4357/aaf85a)[,](https://ui.adsabs.harvard.edu/abs/2019ApJ...871..236A/abstract) [871, 236](https://ui.adsabs.harvard.edu/abs/2019ApJ...871..236A/abstract)
- Allen, W. D., et al. 2005, INTDER 2005: General Program, Which Performs Vibrational Analysis and Higher-Order Non-Linear Transformations
- Altwegg, K., Balsiger, H., & Fuselier, S. A. 2019, [ARA&A,](https://doi.org/10.1146/annurev-astro-091918-104409) [57, 113](https://ui.adsabs.harvard.edu/abs/2019ARA&A..57..113A/abstract)
- Altwegg, K. & Team, R. 2018, in IAU Symp. 332, Astrochemistry VII: Through the Cosmos from Galaxies to Planets, ed. M. Cunningham, T. Millar, & Y. Aikawa (Cambridge: Cambridge Univ. Press), [153](https://ui.adsabs.harvard.edu/abs/2018IAUS..332..153A/abstract)
- Bennett, C. J., Ennis, C. P., & Kaiser, R. I. 2014, [ApJ,](https://doi.org/10.1088/0004-637X/794/1/57) [794, 57](https://ui.adsabs.harvard.edu/abs/2014ApJ...794...57B/abstract)
- Bennett, C. J., Jamieson, C., Mebel, A. M., & Kaiser, R. I. 2004, [PCCP,](https://doi.org/10.1039/b315626p) [6, 735](https://ui.adsabs.harvard.edu/abs/2004PCCP....6..735B/abstract)
- Bennett, C. J., Jamieson, C. S., & Kaiser, R. I. 2008, [P&SS,](https://doi.org/10.1016/j.pss.2008.05.001) [56, 1181](https://ui.adsabs.harvard.edu/abs/2008P&SS...56.1181B/abstract)
- Bieler, A., Altwegg, K., Balsiger, H., et al. 2015, [Natur,](https://doi.org/10.1038/nature15707) [526, 678](https://ui.adsabs.harvard.edu/abs/2015Natur.526..678B/abstract)
- Bizzocchi, L., Lattanzi, V., Laas, J., et al. 2017, [A&A](https://doi.org/10.1051/0004-6361/201730638), [602, A34](https://ui.adsabs.harvard.edu/abs/2017A&A...602A..34B/abstract)
- Cottin, H., & Fray, N. 2008, [SSRv,](https://doi.org/10.1007/s11214-008-9399-z) [138, 179](https://ui.adsabs.harvard.edu/abs/2008SSRv..138..179C/abstract)
- Dubois, D., Sciamma-O'Brien, E., & Fortenberry, R. C. 2019, [ApJ,](https://doi.org/10.3847/1538-4357/ab345e) [883, 109](https://ui.adsabs.harvard.edu/abs/2019ApJ...883..109D/abstract)
- Dulieu, F., Minissale, M., & Bockelée-Morvan, D. 2017, [A&A](https://doi.org/10.1051/0004-6361/201628445), [597, A56](https://ui.adsabs.harvard.edu/abs/2017A&A...597A..56D/abstract)
- Eistrup, C., & Walsh, C. 2019, [A&A](https://doi.org/10.1051/0004-6361/201833380), [621, A75](https://ui.adsabs.harvard.edu/abs/2019A&A...621A..75E/abstract)
- Finney, B., Fortenberry, R. C., Francisco, J. S., & Peterson, K. A. 2016, [JChPh](https://doi.org/10.1063/1.4963337)[,](https://ui.adsabs.harvard.edu/abs/2016JChPh.145l4311F/abstract) [145, 124311](https://ui.adsabs.harvard.edu/abs/2016JChPh.145l4311F/abstract)
- Fortenberry, R. C., & Francisco, J. S. 2017, [ApJ,](https://doi.org/10.3847/1538-4357/aa582d) [835, 243](https://ui.adsabs.harvard.edu/abs/2017ApJ...835..243F/abstract)
- Fortenberry, R. C., Huang, X., Francisco, J. S., Crawford, T. D., & Lee, T. J. 2012, [JChPh](https://doi.org/10.1063/1.4729309), [136, 234309](https://ui.adsabs.harvard.edu/abs/2012JChPh.136w4309F/abstract)
- Fortenberry, R. C., Lee, T. J., & Layfield, J. P. 2017, [JChPh](https://doi.org/10.1063/1.5013026), [147, 221101](https://ui.adsabs.harvard.edu/abs/2017JChPh.147v1101F/abstract)
- Fortenberry, R. C., Trabelsi, T., Westbrook, B. R., Del Rio, W. A., & Francisco, J. S. 2019, [JChPh](https://doi.org/10.1063/1.5102073), [150, 201103](https://ui.adsabs.harvard.edu/abs/2019JChPh.150t1103F/abstract)
- Franz, J., Francisco, J. S., & Peyerimhoff, S. D. 2009, [JChPh,](https://doi.org/10.1063/1.3080808) [130, 084304](https://ui.adsabs.harvard.edu/abs/2009JChPh.130h4304F/abstract)
- Frisch, M. J., Trucks, G. W., Schlegel, H. B., et al. 2009, Gaussian 09 Revision D.01 (Wallingford, CT: Gaussian, Inc.)
- Fuente, A., Goicoechea, J. R., Pety, J., et al. 2017, [ApJL](https://doi.org/10.3847/2041-8213/aaa01b), [851, 49](https://ui.adsabs.harvard.edu/abs/2017ApJ...851L..49F/abstract)
- <span id="page-6-0"></span>Fuselier, S., Altwegg, K., Balsiger, H., et al. 2016, [MNRAS,](https://doi.org/10.1093/mnras/stw2149) [462, S67](https://ui.adsabs.harvard.edu/abs/2016MNRAS.462S..67F/abstract)
- Gaw, J. F., Willets, A., Green, W. H., & Handy, N. C. 1991, in Advances in Molecular Vibrations and Collision Dynamics, ed. J. M. Bowman & M. A. Ratner (Greenwich, CT: JAI Press, Inc.), [170](https://ui.adsabs.harvard.edu/abs/1991amvb.conf..169G/abstract)
- Gerakines, P., Schutte, W., & Ehrenfreund, P. 1996, A&A, [312, 289](https://ui.adsabs.harvard.edu/abs/1996A&A...312..289G/abstract)
- Glinski, R. J., Ford, B. J., Harris, W. M., Anderson, C. M., & Morgenthaler, J. P. 2004, [ApJ](https://doi.org/10.1086/379762), [608, 601](https://ui.adsabs.harvard.edu/abs/2004ApJ...608..601G/abstract)
- Hehre, W. J., Ditchfeld, R., & Pople, J. A. 1972, [JChPh,](https://doi.org/10.1063/1.1677527) [56, 2257](https://ui.adsabs.harvard.edu/abs/1972JChPh..56.2257H/abstract)
- Heritier, K. L., Altwegg, K., Berthelier, J.-J., et al. 2018, [NatCo](https://doi.org/10.1038/s41467-018-04972-5), [9, 2580](https://ui.adsabs.harvard.edu/abs/2018NatCo...9.2580H/abstract)
- Herzberg, G. 1966, Electronic Spectra and Electronic Structure of Polyatomic Molecules (New York: Van Nostrand)
- Hill, J. G., & Peterson, K. A. 2010, [PCCP](https://doi.org/10.1039/c0cp00020e), [12, 10460](https://ui.adsabs.harvard.edu/abs/2010PCCP...1210460H/abstract)
- Huang, X., Taylor, P. R., & Lee, T. J. 2011, [JPCA](https://doi.org/10.1021/jp2019704), [115, 5005](https://ui.adsabs.harvard.edu/abs/2011JPCA..115.5005H/abstract)
- Huntress, W., Jr, Alien, M., & Delrtsky, M. 1991, [Natur,](https://doi.org/10.1038/352316a0) [352, 316](https://ui.adsabs.harvard.edu/abs/1991Natur.352..316H/abstract)
- Jamieson, C. S., Mebel, A. M., & Kaiser, R. I. 2006, [Chem. Phys. Chem.](https://doi.org/10.1002/cphc.200600390), 7, 2508
- Jamieson, C. S., Mebel, A. M., & Kaiser, R. I. 2007a, [CPL,](https://doi.org/10.1016/j.cplett.2007.06.009) [443, 49](https://ui.adsabs.harvard.edu/abs/2007CPL...443...49J/abstract)
- Jamieson, C. S., Mebel, A. M., & Kaiser, R. I. 2007b, [CPL](https://doi.org/10.1016/j.cplett.2007.04.043), [440, 105](https://ui.adsabs.harvard.edu/abs/2007CPL...440..105J/abstract)
- Jamieson, C. S., Mebel, A. M., & Kaiser, R. I. 2008, [CPL](https://doi.org/10.1016/j.cplett.2007.11.052), [450, 312](https://ui.adsabs.harvard.edu/abs/2008CPL...450..312J/abstract)
- Knizia, G., Adler, T. B., & Werner, H.-J. 2009, [JChPh](https://doi.org/10.1063/1.3054300), [130, 054104](https://ui.adsabs.harvard.edu/abs/2009JChPh.130e4104K/abstract)
- Laufer, D., Bar-Nun, A., & Ninio Greenberg, A. 2018, [MNRAS](https://doi.org/10.1093/mnras/stx3359), [469, S818](https://ui.adsabs.harvard.edu/abs/2017MNRAS.469S.818L/abstract)
- Lipp, M., Evans, W., Garcia-Baonza, V., & Lorenzana, H. 1998, [JLTP,](https://doi.org/10.1023/A:1022267115640) [111, 247](https://ui.adsabs.harvard.edu/abs/1998JLTP..111..247L/abstract)
- Luspay-Kuti, A., Mousis, O., Lunine, J. I., et al. 2018, [SSRv,](https://doi.org/10.1007/s11214-018-0541-2) [214, 115](https://ui.adsabs.harvard.edu/abs/2018SSRv..214..115L/abstract)
- Martin, J. M. L., & Taylor, P. R. 1997, [AcSpA](https://doi.org/10.1016/S1386-1425(96)01869-0), [53, 1039](https://ui.adsabs.harvard.edu/abs/1997AcSpA..53.1039M/abstract)
- Martín-Doménech, R., Manzano-Santamaría, J., Caro, G. M., et al. 2015, [A&A,](https://doi.org/10.1051/0004-6361/201526003) [584, A14](https://ui.adsabs.harvard.edu/abs/2015A&A...584A..14M/abstract)
- Meredith, C., Hamilton, T. P., & Schaefer, H. F., III 1992, [JPC,](https://doi.org/10.1021/j100202a034) 96, 9250
- Mills, I. M. 1972, in Molecular Spectroscopy—Modern Research, ed. K. N. Rao & C. W. Mathews (New York: Academic), [115](https://ui.adsabs.harvard.edu/abs/1972msmr.conf..115M/abstract)
- Moll, N. G., Clutter, D. R., & Thompson, W. E. 1966, [JChPh,](https://doi.org/10.1063/1.1727526) [45, 4469](https://ui.adsabs.harvard.edu/abs/1966JChPh..45.4469M/abstract)
- Møller, C., & Plesset, M. S. 1934, [PhRv](https://doi.org/10.1103/PhysRev.46.618), [46, 618](https://ui.adsabs.harvard.edu/abs/1934PhRv...46..618M/abstract)
- Mousis, O., Ronnet, T., Lunine, J., et al. 2018, [ApJ](https://doi.org/10.3847/1538-4357/aab6b9), [858, 66](https://ui.adsabs.harvard.edu/abs/2018ApJ...858...66M/abstract)
- Papousek, D., & Aliev, M. R. 1982, Molecular Vibration-Rotation Spectra (Amsterdam: Elsevier)
- Pierce, D. M., & A'Hearn, M. F. 2010, [ApJ](https://doi.org/10.1088/0004-637X/718/1/340), [718, 340](https://ui.adsabs.harvard.edu/abs/2010ApJ...718..340P/abstract)
- Radhakrishnan, S., Gudipati, M. S., Sander, W., & Lignell, A. 2018, [ApJ](https://doi.org/10.3847/1538-4357/aad4a6)[,](https://ui.adsabs.harvard.edu/abs/2018ApJ...864..151R/abstract) [864, 151](https://ui.adsabs.harvard.edu/abs/2018ApJ...864..151R/abstract)
- Raghavachari, K., Trucks, G. W., Pople, J. A., & Head-Gordon, M. 1989, [CPL](https://doi.org/10.1016/S0009-2614(89)87395-6)[,](https://ui.adsabs.harvard.edu/abs/1989CPL...157..479R/abstract) [157, 479](https://ui.adsabs.harvard.edu/abs/1989CPL...157..479R/abstract)
- Rothman, L. S., Hawkins, R. L., Wattson, R. B., & Gamache, R. R. 1992, [JQSRT](https://doi.org/10.1016/0022-4073(92)90119-O), [48, 537](https://ui.adsabs.harvard.edu/abs/1992JQSRT..48..537R/abstract)
- Shimanouchi, T. 1972, Tables of Molecular Vibrational Frequencies, Vol. 1 (39th ed.; Washington, DC: National Standards Reference Data System)
- Taquet, V., Furuya, K., Walsh, C., & van Dishoeck, E. F. 2016, [MNRAS](https://doi.org/10.1093/mnras/stw2176)[,](https://ui.adsabs.harvard.edu/abs/2016MNRAS.462S..99T/abstract) [462, S99](https://ui.adsabs.harvard.edu/abs/2016MNRAS.462S..99T/abstract)
- Theis, R. A., & Fortenberry, R. C. 2016, [MolAs,](https://doi.org/10.1016/j.molap.2015.12.001) [2, 18](https://ui.adsabs.harvard.edu/abs/2016MolAs...2...18T/abstract)
- Wagner, J. P., McDonald, D. C., II, & Duncan, M. A. 2018, [Angew. Chem. Int.](https://doi.org/10.1002/anie.201802093) [Ed.,](https://doi.org/10.1002/anie.201802093) 57, 5081
- Watson, J. K. G. 1977, in Vibrational Spectra and Structure, ed. J. R. During (Amsterdam: Elsevier), 1
- Werner, H.-J., Knowles, P. J., Knizia, G., Manby, F. R., & Schütz, M. 2012, [WIREs Comput. Mol. Sci,](https://doi.org/10.1002/wcms.82) 2, 242
- Werner, H.-J., Knowles, P. J., Knizia, G., et al. 2015, MOLPRO, Version 2015.1, a Package of ab Initio Programs, http://[www.molpro.net](http://www.molpro.net)
- Xie, Y., Allen, W. D., Yamaguchi, Y., & Schaefer, H. F., III 1996, [JChPh](https://doi.org/10.1063/1.471470)[,](https://ui.adsabs.harvard.edu/abs/1996JChPh.104.7615X/abstract) [104, 7615](https://ui.adsabs.harvard.edu/abs/1996JChPh.104.7615X/abstract)
- Yao, Y., & Giapis, K. P. 2017, [NatCo,](https://doi.org/10.1038/ncomms15298) [8, 15298](https://ui.adsabs.harvard.edu/abs/2017NatCo...815298Y/abstract)
- Yu, Q., Bowman, J. M., Fortenberry, R. C., et al. 2015, [JPCA,](https://doi.org/10.1021/acs.jpca.5b09682) [119, 11623](https://ui.adsabs.harvard.edu/abs/2015JPCA..11911623Y/abstract)
- Zhao, D., Doney, K. D., & Linnartz, H. 2014, [ApJL](https://doi.org/10.1088/2041-8205/791/2/L28), [791, L28](https://ui.adsabs.harvard.edu/abs/2014ApJ...791L..28Z/abstract)
- Zheng, W., Jewitt, D., & Kaiser, R. I. 2006, [ApJ](https://doi.org/10.1086/499231), [639, 534](https://ui.adsabs.harvard.edu/abs/2006ApJ...639..534Z/abstract)